



where

$$p_{n,\alpha}^{\alpha}(x) = \frac{\binom{n}{k} \prod_{s=0}^{k-1} (x + \alpha s) \prod_{s=0}^{n-k-1} (1-x + \alpha s)}{\prod_{s=0}^{n-1} (1 + \alpha s)} \quad \dots (1.3)$$

We get the Bernstein polynomials by putting  $\alpha = \beta = 0$ , starting with two parameters  $\alpha$  &  $\beta$  satisfying  $0 \leq \alpha \leq \beta$  in 1983.

The other generalization of Stancu Operators was given in [8] and studied the linear positive operators as follows-

$$S_n^{\alpha,\beta}(f, x) = \sum_{k=0}^n p_{n,k}(x) f\left(\frac{k+\alpha}{n+\beta}\right), \quad 0 \leq x \leq 1 \quad \dots (1.4)$$

where

$$p_{n,k}(x) = \binom{n}{k} x^k (1-x)^{n-k}, \quad \dots (1.5)$$

It is the Bernstein basis function.

Recently Ibrahim [5] introduced Stancu Chlodowsky polynomials and investigated convergence and approximation properties of these operators.

Now Stancu type generalization for Operators (1.1) as follows-

$$P_n^{\alpha,\beta}(f, x) = \sum_{v=0}^{n-1} b_{n,v}(x) \int_0^{\infty} p_{n,v}(t) f\left(\frac{nt+\alpha}{n+\beta}\right) dt, \quad x \in [0, \infty] \quad \dots (1.6)$$

where  $b_{n,v}(x)$  and  $p_{n,v}(t)$  are defined as earlier. The operators  $P_n^{(\alpha,\beta)}$  are called Modified Beta Stancu Operators. For  $\alpha = \beta = 0$ , the operators (1.2) reduce to operators (1.1).

It is easily verified that the operators  $P_n$  are linear positive operators. Also  $P$

For  $d_0, d_1, d_2, \dots, d_v$  arbitrary but fixed distinct positive integers, the linear combination  $P_n(f, v, x)$  of  $P_d j_n(f, x), j = 0, 1, 2, \dots, n$  are defined by

$$P_n(f, v, x) = \sum_{j=0}^v C(j, v) P_{d,jn}(f, x) \quad \dots (1.7)$$

where  $C(j, v) = \prod_{i=0, i \neq j}^v \frac{\alpha_j}{\alpha_i - \alpha_j}$ ,  $v \neq 0$  and  $C(0,0) = 1$

Alternately the above linear combination may be defined as-

$$P_n(f, v, x) = \begin{vmatrix} 1 & d^{-1} & d^{-2} & \dots & d^{-v} \\ \vdots & \vdots & \vdots & \dots & \vdots \\ 1 & d^{-1} & d^{-2} & \dots & d^{-v} \\ \vdots & \vdots & \vdots & \dots & \vdots \\ 1 & d^{-1} & d^{-2} & \dots & d^{-v} \end{vmatrix} \begin{vmatrix} P_{d,n} & d^{-1} & d^{-2} & \dots & d^{-v} \\ \vdots & \vdots & \vdots & \dots & \vdots \\ P_{d,n} & d^{-1} & d^{-2} & \dots & d^{-v} \\ \vdots & \vdots & \vdots & \dots & \vdots \\ P_{d,n} & d^{-1} & d^{-2} & \dots & d^{-v} \end{vmatrix}, \quad \dots (1.8)$$

## 2. BASIC RESULTS

In this section, we study some definitions and certain lemmas by using Stancu operators to prove our main theorems. We shall extend the results of Maheshwari and Gupta [6] by applying Stancu type of generalization.

Here we mention two definitions named as Steklov mean and  $k^{\text{th}}$  order modulus of continuity, which will be beneficial in finding our results.

**Steklov Mean-** Let us assume that  $0 < a < a_1 < b_1 < \infty$ , for sufficiently small  $\delta > 0$ , the  $(2k + 2)^{\text{th}}$  order.

Steklov mean  $g_{2k+2, i\delta}$  corresponding to  $g \in C_y[0, \infty)$  is defined by

$$g_{2k+2, \delta}(t) = \delta^{-(2k+2)} \int_{\delta/2}^{\delta/2} \int_{\delta/2}^{\delta/2} \dots \int_{\delta/2}^{\delta/2} [g(t) - \Delta^{2k+2} g(t)] dt, \quad 2k+2$$

where  $\delta = \frac{1}{2k+2} \sum_{i=1}^{2k+2} \delta_i$  and  $\delta_i \in [a, b]$

It is easily checked [2, 3, 5] that

- i.  $g_{2k+2, \delta}$  has continuous derivatives up to order  $(2k + 2)$  on  $[a, b]$ .
- ii.  $\|g^{(r)}\|_{C[a, b]} \leq K \delta^r (g, \delta, a, b), \quad r = 1, 2, \dots, (2k + 2),$
- iii.  $\|g - g_{2k+2, \delta}\|_{C[a, b]} \leq K W_{2k+2}(g, \delta, a, b),$
- iv.  $\|g_{2k+2, \delta}\|_{C[a, b]} \leq K \|g\|_y$

where 'K' is an arbitrary constant and in this paper it will have different values at different places.

**Order Modulus of Continuity-** The  $k^{\text{th}}$  order moment of continuity  $m_k(f, \delta)$  for a function continuous on an interval  $[a, b]$  is defined by

$$m_k(f, \delta) = \text{Sup} \{ |\Delta^k f(x)| : |h| \leq \delta, x, x + kh \in I \}$$

For  $k = 1, m_k(f, \delta)$  is written simply as  $m_1(\delta)$  or  $m(f, \delta)$ .

**Lemma-2.1** – For  $m \in N \cup \{0\}$  if

$$U_{n,m}(x) = \sum_{v=0}^{\infty} b_{n,v}(x) \left( \frac{v}{n} - x \right)^m$$

then  $(n+1)U_{n,m+1}(x) = x(1+x) \{ U_{n,m}(x) + m U_{n,m+1}(x) \}$

**Consequently**

- (i)  $U_{n,m}(x)$  is a polynomial in  $x$  of degree  $\leq m$ .
- (ii)  $U_{n,m}(x) = O(n^{-[m+1/2]})$ , Where  $[\epsilon]$  denotes the integral part of  $\epsilon$ .

**Lemma-2.2-** Let the  $N^{\text{th}}$  order moment be defined by

$$T_{n,N}(x) = \frac{n-1}{n} \sum_{v=0}^{\infty} b_{n,v}(x) \int_0^{\infty} p_{n,v}(t) \left(\frac{nt+\alpha}{n+b} - x\right)^N dt \quad \dots (1.5)$$

then  $T_{n,0}(x) = 1$ ,  $T_{n,1}(x) = \frac{\alpha}{n+b} - x$  and

$$(n-N-2)T_{n,N+1} = x(1+x)[T'_{n,N}(x) + 2NT_{n,N-1}(x)] + [(1+x)(N+1) + x]T_{n,N}(x),$$

$n > N + 2$

Further, for all  $x \in [0, \infty)$ ,  $T_{n,m}(x) = O\left(\frac{1}{n^{-(m+1)^2}}\right)$

**ROOF:** The proof of Lemma-2.1 can easily be obtained by using the definition of  $T_{n,N}(x)$  from Lemma-2.2. so, first, for the proof of Lemma-2.2 we proceed as follows.

Differentiating (1.5) with respect to  $x$  and multiplying by  $x(1+x)$  on both sides-

$$xT'_{n,N-1}(x) = \frac{n-1}{n} \sum_{v=0}^{\infty} b_{n,v}(x) \int_0^{\infty} p_{n,v}(t) \left(\frac{nt+\alpha}{n+b} - x\right)^{N-1} dt$$

**Using relations**

1)  $x(1+x)b'_{n,v}(x) = [v - (n+1)x]b_{n,v}(x)$ ,

$$\frac{nt+\alpha}{n+b} - x = \frac{nt+\alpha}{n+b} - \frac{nt+\alpha}{n+b} + x = \frac{nt+\alpha}{n+b} - \frac{nt+\alpha}{n+b} + x$$

3)  $\frac{n-1}{n} \sum_{v=0}^{\infty} b_{n,v}(x) \int_0^{\infty} p'_{n,v}(t) \left(\frac{nt+\alpha}{n+b} - x\right)^N dt$   
 $= -\frac{n-1}{n} \sum_{v=0}^{\infty} b_{n,v}(x) \int_0^{\infty} p_{n,v}(t) \left(\frac{nt+\alpha}{n+b} - x\right)^{N-1} dt$   
 $= -NT_{n,N-1}(x)$

we obtain-

$$\begin{aligned}
& x(1+x)[T'_{n,N}(x) + NT_{n,N-1}(x)] \\
&= \frac{n-1}{n} \sum_{v=0}^{\infty} [v - (n+1)x] b_{n,v}(x) \int_0^{\infty} p_{n,v}(t) \left(\frac{nt+\alpha}{n+\beta} - x\right)^n dt \\
&= \frac{n-1}{n} \sum_{v=0}^{\infty} b_{n,v}(x) \int_0^{\infty} \left[ \left(v - n\frac{nt+\alpha}{n+\beta}\right) + n\left(\frac{nt+\alpha}{n+\beta} - x\right) - x \right] p_{n,v}(t) \left(\frac{nt+\alpha}{n+\beta} - x\right)^m dt \\
&= \frac{n-1}{n} \sum_{v=0}^{\infty} b_{n,v}(x) \int_0^{\infty} \frac{nt+\alpha}{n+\beta} \left(1 + \frac{nt+\alpha}{n+\beta}\right) p'_{n,v}(t) \left(\frac{nt+\alpha}{n+\beta} - x\right)^n dt + nT_{n,N+1}(x) \\
&\quad - xT_{n,N}(x) \\
&= \frac{n-1}{n} \sum_{v=0}^{\infty} b_{n,v}(x) \int_0^{\infty} \left[ (1+2x) \left(\frac{nt+\alpha}{n+\beta} - x\right) + \left(\frac{nt+\alpha}{n+\beta} - x\right)^2 \right. \\
&\quad \left. + x(1+x) \right] p_{n,v}(t) \left(\frac{nt+\alpha}{n+\beta} - x\right)^m dt + nT_{n,N+1}(x) - xT_{n,N}(x) \\
&= (1+2x) \frac{n-1}{n} \sum_{v=0}^{\infty} b_{n,v}(x) \int_0^{\infty} p'_{n,v}(t) \left(\frac{nt+\alpha}{n+\beta} - x\right)^{m+1} dt \\
&\quad + \frac{n-1}{n} \sum_{v=0}^{\infty} b_{n,v}(x) \int_0^{\infty} p'_{n,v}(t) \left(\frac{nt+\alpha}{n+\beta} - x\right)^{m+2} dt \\
&\quad + x(1+x) \frac{n-1}{n} \sum_{v=0}^{\infty} b_{n,v}(x) \int_0^{\infty} p'_{n,v}(t) \left(\frac{nt+\alpha}{n+\beta} - x\right)^m dt + nT_{n,N+1}(x) \\
&\quad - xT_{n,N}(x) \\
&= -(N+1)(1+2x)T_{n,N}(x) - (N+2)T_{n,N+1}(x) - Nx(1+x)T_{n,N-1}(x) \\
&\quad + nT_{n,N+1}(x) - xT_{n,N}(x)
\end{aligned}$$

This leads to Lemma-2.2. Obviously  $T_{n,m}(x) = O\left(n^{-[m+1]^2}\right)$

**Lemma-2.3-** There exists the polynomial  $q_{i,j,r}(x)$  independent of  $n$  &  $v$ , such that

$$x^r (1+x)^r \frac{d^r}{dx^r} (x^v (1+x)^{-n-v}) = \sum_{\substack{2i+j \leq r \\ i, j \geq 0}} n^i (v-nx)^j q_{i,j,r}(x) x^v (1+x)^{-n-v}$$

**Lemma-2.4-** Let  $f$  be  $r$  times differentiable on  $[0, \infty)$  such  $f^{(r-1)} = O(t^\alpha)$  for some  $\alpha > 0$  as  $t \rightarrow \infty$  then

for  $r = 1, 2, 3$  and  $n > \alpha + r$ , we have

$$\frac{1}{n} \sum_{v=0}^{\infty} \frac{f^{(n-v)}(x)}{(n-v)!} \binom{n}{v} x^v (1+x)^{-n-v} = \frac{f(x)}{(n+\alpha)} + o\left(\frac{1}{n}\right)$$

**PROOF-** We have

$$\frac{1}{n} \sum_{v=0}^{\infty} \frac{f^{(n-v)}(x)}{(n-v)!} \binom{n}{v} x^v (1+x)^{-n-v} = \frac{f(x)}{(n+\alpha)} + o\left(\frac{1}{n}\right)$$

By using Leibnitz theorem-

$$\begin{aligned}
 \Pr(f, x) &= \frac{n-1}{n} \sum_{i=0}^{\infty} \sum_{v=i}^{\infty} \binom{r}{i} \frac{r(n+v+r-i)!}{(n-1)!(v-i)!} (-1)^{r-i} x^{v-i} (1+x)^{-n-v-1-r-i} \int_0^{\infty} p_{n,v}^{r-i}(t) f\left(\frac{nt+\alpha}{n+\beta}\right) dt \\
 &= \frac{n-1}{n} \sum_{v=0}^{\infty} \frac{(n+v+r)!}{(n-1)!v!} \frac{x^v}{(1+x)^{n+v+r+1}} \int_0^{\infty} \sum_{i=0}^r (-1)^{r-i} \binom{r}{i} p_{n,v+i}(t) f\left(\frac{nt+\alpha}{n+\beta}\right) dt \\
 &= \frac{(n-1)(n+r-1)!}{(n)!} \sum_{v=0}^{\infty} \frac{n+r,v}{(n-2)!n!} (x) \int_0^{\infty} \sum_{i=0}^r (-1)^{r-i} \binom{r}{i} p_{n,v+i}(t) f\left(\frac{nt+\alpha}{n+\beta}\right) dt
 \end{aligned}$$

Again, by using Leibnitz theorem, we get

$$p_{n-r,v+r}^r(t) = \frac{(n-1)!}{(n-r-1)!} \sum_{i=0}^r (-1)^i \binom{r}{i} p_{n,v+i}(t)$$

Hence,

$$\Pr(f, x) = \frac{(n-r-1)!(n+r-1)!}{(n-2)!n!} \sum_{v=0}^{\infty} \frac{n+r,v}{(n-2)!n!} (x) \int_0^{\infty} \sum_{i=0}^r (-1)^i p_{n-r,v+r}^r(t) f\left(\frac{nt+\alpha}{n+\beta}\right) dt$$

Integrating r times, we get the required result.

**Lemma-2.5** Let  $f \in C_{\nu}[0, \infty)$ , if  $f^{(2k+r+2)}$  exists at a point  $x \in [0, \infty)$ , then

$$\lim_{n \rightarrow \infty} n^{v+1} \left[ \Pr(f, (d_0, d_1, \dots, d_v), x) - f^r(x) \right] = \sum_{i=r}^{2v+r+2} Q(i, v, r, x) f^{(i)}(x)$$

where  $Q(i, v, r, x)$  are certain polynomials in  $x$

### 3. MAIN RESULTS

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In this section we shall prove the following main results.

**Theorem 3.1-** Let  $f^r \in C_y[0, \infty)$  and  $0 < a < a_1 < b_1 < b < \infty$  then for 'n sufficiently large

$$\|P_n^r(f, v, x) - f^r\|_{C[a_1, b_1]} \leq \text{Max}\{C_1 m_{2v+2}(f^r, n^{-1/2}a, b), C_2 n^{-(v+1)} \|f\|_y\}$$

where  $C_1 \equiv C_1(v, r)$  and  $C_2 \equiv C_2(v, r, f)$

**Proof:** First, we have by linearity property of the operators, we have

$$\begin{aligned} \|P_n^r(f, v) - f^n\|_{C[a_1, b_1]} &\leq \|P_n^r(f - f_{2v+2, \delta}^r, v)\|_{C[a_1, b_1]} \\ &+ \|P_n^r(f_{2v+2, \delta}^r(d_0, d_1, \dots, d_v)) - f^n\|_{C[a_1, b_1]} \\ &+ \|f^r - f_{2v+2, \delta}^r\|_{C[a_1, b_1]} \\ &= B_1 + B_2 + B_3, \text{ (Say)} \end{aligned}$$

By property (iii) of Steklov mean, we have

$$B_3 \leq Km_{2v+2}(f^r, \delta, a, b)$$

Next, by Lemma-2.5, we have

$$B_2 \leq Kn^{-(v+1)} \sum_{j=r}^{2v+r+2} \|f_{2v+2, \delta}^j\|_{C[a, b]}$$

By interpolation property due to Goldberg and Meir [2] for each  $j = r, r + 1, \dots, 2v + r + 2$ , we have-

$$\|f_{2v+2, \delta}^j\|_{C[a, b]} \leq K \{ \|f_{2v+2, \delta}\|_{C[a, b]} + \|f_{2v+2, \delta}^{2v+r+2}\|_{C[a, b]} \}$$

Therefore by properties (ii) and (iv) of Steklov mean, we have-

$$B_2 \leq Kn^{-(v+1)} \{ \|f\|_y + \delta^{-(2v+2)} m_{2v+2}(f^r, \delta) \}$$

Finally, we shall estimate B, choosing  $a^*, b^*$  satisfying the conditions,

$$0 < a < a^* < a_1 < b_1 < b^* < \infty$$

Also let  $f$  be a characteristic function of the interval  $[a^*, b^*]$ , then Type equation here.

$$\begin{aligned}
 B &\leq \|\Pr^n [\psi(\frac{nt+\alpha}{n+b})] \{f(\frac{nt+\alpha}{n+b}) - f_{2v+2,\delta}(\frac{nt+\alpha}{n+b})\}\|_{C[a_1,b_1]} \\
 &\quad + \|\Pr^n [\{1 - f(\frac{nt+\alpha}{n+b})\} \{f(\frac{nt+\alpha}{n+b}) - f_{2v+2,\delta}(\frac{nt+\alpha}{n+b})\}\|_{C[a_1,b_1]} \\
 &= B_4 + B_5, \quad (\text{Say})
 \end{aligned}$$

We may note here that to estimate  $B_4$  and  $B_5$ , it is enough to consider their expressions without the linear combinations.

By Lemma-2.4, we have

$$\begin{aligned}
 &\Pr^n [f(\frac{nt+\alpha}{n+b}) \{f(\frac{nt+\alpha}{n+b}) - f_{2v+2,\delta}(\frac{nt+\alpha}{n+b})\}, x] \\
 &= \frac{(n-r-1)!(n+r-1)!}{(n-2)!n!} \int_0^\infty \int_0^\infty (x)^{n-r,v} (t)^{n-r,v+r} f(\frac{nt+\alpha}{n+b}) \{f_{2v+2,\delta}(\frac{nt+\alpha}{n+b})\} dt
 \end{aligned}$$

Hence,

$$\|\Pr^n [f(\frac{nt+\alpha}{n+b}) \{f(\frac{nt+\alpha}{n+b}) - f_{2v+2,\delta}(\frac{nt+\alpha}{n+b})\}, \cdot]\|_{C[a,b]} \geq \|\Pr^n [f_{2v+2,\delta}(\frac{nt+\alpha}{n+b})]\|_{C[a^*,b^*]}$$

Now, for  $x \in [a, b]$  &  $t \in [0, \infty) \setminus [a^*, b^*]$ , we choose a  $\delta$  such that  $|\frac{nt+\alpha}{n+b} - x| \geq \delta$ .

Therefore by Lemma-2.3 and Schwarz inequality, we have-

$$I = P_n \left\{ \left| 1 - f\left(\frac{nt + \alpha}{n + \beta}\right) \right| \left| f\left(\frac{nt + \alpha}{n + \beta}\right) - f_{2v+2,\delta}\left(\frac{nt + \alpha}{n + \beta}\right) \right|, x \right\}$$

$$\leq \frac{n-1}{n} \sum_{\substack{2i+j \leq r \\ i,j \geq 0}} n^i \frac{|q_{i,j,r}(x)|}{x^r(1+x)^r} \sum_{v=0}^{\infty} b_{n,v}(x) \cdot |v - nx|^j \int_0^{\infty} f_{p_{n,v}}(t) \left\{ 1 - f\left(\frac{nt + \alpha}{n + \beta}\right) \right\} \left| f\left(\frac{nt + \alpha}{n + \beta}\right) - f_{2v+2,\delta}\left(\frac{nt + \alpha}{n + \beta}\right) \right| dt$$

$$I = P_n \left\{ \left| 1 - f\left(\frac{nt + \alpha}{n + \beta}\right) \right| \left| f\left(\frac{nt + \alpha}{n + \beta}\right) - f_{2v+2,\delta}\left(\frac{nt + \alpha}{n + \beta}\right) \right|, x \right\}$$

$$\leq \frac{n-1}{n} \sum_{\substack{2i+j \leq r \\ i,j \geq 0}} n^i \frac{|q_{i,j,r}(x)|}{x^r(1+x)^r} \sum_{v=0}^{\infty} b_{n,v}(x) \cdot |v - nx|^j \int_0^{\infty} f_{p_{n,v}}(t) \left\{ 1 - f\left(\frac{nt + \alpha}{n + \beta}\right) \right\} \left| f\left(\frac{nt + \alpha}{n + \beta}\right) - f_{2v+2,\delta}\left(\frac{nt + \alpha}{n + \beta}\right) \right| dt$$

$$\leq K \|f\|_y \left( \frac{n-1}{n} \sum_{\substack{2i+j \leq r \\ i,j \geq 0}} n^i \sum_{v=0}^{\infty} b_{n,v}(x) |v - nx|^j \int_0^{\infty} f_{p_{n,v}}(t) dt \right) \left| \frac{nt + \alpha}{n + \beta} - x \right|$$

$$\geq \delta_1$$

$$\leq K \delta_1^{-2c} \|f\|_y \frac{n-1}{n} \sum_{\substack{2i+j \leq r \\ i,j \geq 0}} n^i \sum_{v=0}^{\infty} b_{n,v}(x) |v - nx|^j \int_0^{\infty} f_{p_{n,v}}(t) dt$$

$$\leq K \delta_1^{-2c} \|f\|_y \sum_{\substack{2i+j \leq r \\ i,j \geq 0}} n^i \left( \sum_{v=0}^{\infty} b_{n,v}(x) (v - nx)^j \int_0^{\infty} f_{p_{n,v}}(t) dt \right) \left( \frac{nt + \alpha}{n + \beta} - x \right)^{4c}$$

$$\leq K \delta_1^{-2c} \|f\|_y \sum_{\substack{2i+j \leq r \\ i,j \geq 0}} n^i \left( \sum_{v=0}^{\infty} b_{n,v}(x) (v - nx)^j \int_0^{\infty} f_{p_{n,v}}(t) dt \right) \left( \frac{nt + \alpha}{n + \beta} - x \right)^{4c}$$

Hence, by Lemma-2.1 & 2.2, we have-

$$|1 \leq K \|f\|_y O(n)^{1+\frac{1}{z}+c} \leq K n^{-y} \|f\|_y$$

Where  $q = (s - n/2)$ . Now choose  $\delta > 0$  such  $q \geq (v + 1)$ , then

$$I \leq K n^{-(v+1)} \|f\|_y$$

Therefore by property (iii) of Steklov mean, we get-

$$\begin{aligned} B_1 &\leq K \|f^r - f_{2v+2,\delta}^r\|_{C[a^*,b^*]} + K n^{-(v+1)} \|f\|_y \\ &\leq K m_{2v+2}(f^r, \delta, a, b) + K n^{-(v+1)} \|f\|_y \end{aligned}$$

Hence with  $\delta = n^{-1/2}$ , the theorem follows.

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